Prospectus for Levels of Idealism

O The purpose of this brief essay is to outline a planned book-length study (tentatively entitled Levels of Idealism) of certain evolving patterns in the metaphysics of Berkeley, Hume and Kant.

When finished, the projected manuscript would consist of three sixty-to-eighty-page central chapters on the three philosophers considered, framed by a twenty-page introduction and conclusion. A separate expository appendix would provide a brief glossary (with references for further reading) of the the basic metalogical arguments and notation employed (The metalogical 'quotation-marks' " ... ", for example, which appear a couple of times below, are motivated by Gödel's coding-arguments; they provide a formal counterpart of the traditional distinction between use and mention).

- 1 Very roughly, the basic idea behind the manuscript's proposed title is that Berkeley can be regarded as a 'first-order,' and Hume a 'second-order' idealist (where the 'orders' are taken in the metalogical sense of this word), and Kant as a kind of indefinitely-higher-order ('transcendental') idealist, who believed he could formulate a 'transcendental deduction' of the following principal assertions:
- 1.1 that there 'must' exist a unique (meta)theoretical stratification
 of "Erscheinungen" ("appearances") into "Anschauungen"
 ("intuitions") and "Begriffe" ("concepts"), his counterpart(s)
 of empirical "impressions" and "ideas;"
- 1.2 that each of these levels is, roughly speaking, semantically complete ("durchgängig bestimmt" / "thoroughgoingly determined");
- 1.3 that such 'completeness'(Bestimmtheit; Vollständigkeit")
 'must' be dictated by a unique background model or interpretation
 E of theoretical "Erfahrung" ("experience");
- 1.4 that the isomorphism-type of this interpretation E is both
 "constitutive" of human "Verstand" ("understanding"), and
 coextensive with it;

- 1.5 that there 'must' also exist another stratification, this time of Lockean "ideas of reflexion," and partly parallel at least to the one described in 1.1 (textual evidence for this can be found in passages from the First Critique such as the ones cited below in 4), into "Verstandesbegriffe" ("concepts of the understanding") and "Vernunftideen" ("ideas of reason"); and finally
- 1.6 that the second stratification in 1.5 is **not** uniquely determined by an interpretation comparable to E above, so that ideas of reason ramify in underdetermined and undecidable ways (in the four Antinomies, for example; or in 'proofs' for the existence of god).
- 1.7 On my interpretation, then, close analogies can be traced between Berkeley's first-order "immaterialism" and Hume's second-order "irrelationism." The latter, moreover, leads quite naturally to Kant's more complex and elusively higher-order denial that there is any perspective within "experience" which can clarify an intelligible distinction between "('the') appearances," and whatever it is they (allegedly) represent (the "things in themselves").
- 1.8 These opening paragraphs, in effect, have provided an outline of the book's introduction. A prototype of the Hume-chapter ("The Second-order Idealism of David Hume")already exists, and I hope to complete a draft of the Berkeley-chapter this year.

The next three numbered sections offer a brief sketch of some of the ideas of the Berkeley-chapter, followed by somewhat longer outlines of the basic ideas of those devoted to Hume and Kant.

- 2 The treatment of **Berkeley** in the first of the book's three central chapters will explore (among other things) the implications of an extended analogy between
- 2.1 two alternative readings of the notorious 'master'-argument
 (the one about the 'tree in the quad;' it is a "park" not a
 quadrangle in Berkeley's text, and he never called his

thought-experiment "master-"; though he did clearly consider it compelling, and perhaps decisive):

- 2.1.1 one which employs a 'strong,' 'extensional' counterpart of Berkeley's notion of "perception"/"conception" (essentially as definability); and
- 2.1.2 a second which involves a 'weaker,' 'intensional' gloss
 of this vexed notion (essentially as internally-coded consistency)
 and
- 2.2 metatheoretic implications of
- 2.2.1 the Berry / Richard paradox, which arises when one tries to 'define,' e. g., the least integer not 'definable' in less than 10^{65} syllables (this number is sometimes cited as a bound on 'the' number of electrons in the known physical universe), and
- 2.2,2 Gödels (second incompleteness) theorem, which establishes (on one reading of formalized 'conceivability') that many interesting theories can 'conceive' of many states of affairs which are both 'inconceivable' and the case.
- 2.3 In other sections of this projected chapter, I will explore related implications of these and other metamathematical ideas,
- 2.3.1 for Berkeley's critique of abstraction;
- 2.3.2 for his surprisingly latitudinarian doctrine of "signs"
 (set forth briefly in the Principles, and in more detail in
 Alciphron); and
- 2.3.3 for the rigoristic finitism which underlay both Berkeley's metaphysics and his philosophy of mathematics, including his cogent critique of contemporary rationales for the differential and integral calculus (a subject the Germans, perhaps revealingly, still call Infinitesimalrechnung).

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I originally drafted the hundred-page essay-chapter enclosed ("The Second-Order Idealism of David Hume") as a long independent paper, and I intend to submit a thirty-page excerpt from it to a journal. About eighty laser-printed pages of the present version -- with some material transferred to an initial discussion

of parallel ideas in Berkeley, and a few pages at the end relocated in the chapter on Kant -- would form the second chapter of the projected book.

- 3.1 According to the view I set forth in this essay, Hume was in fact not a skeptic in the classical (academic or pyrrhonist) senses of the word, but rather a 'second-order idealist:' a reductive metaphysician who appealed to implicit Berkeleyan "maxims" and "principles" to reject not first-order mind-independent objects (which he regarded with kind of benign neglect); but second-order mind-independent relations ("necessity," "causation") between such objects.
- 3.2 In the sense in which Berkeley called himself an 'immaterialist,' therefore, one might appropriately call Hume an 'irrelationist.'

 To the extent this interpretation is tenable, one can also attempt to draw from it some obvious and fairly extensive implications for Hume's claim to advocate a "consequent skepticism," and I do this in the essay at some length.

Berkeley, of course, sincerely opposed skepticism, and never attempted the sort of metacritique of his own methodological assumptions, maxims and "principles" that characterized academic and pyrrhonist skepticism, beyond the dialectical rebuttals set forth in the **Principles** and **Dialogues**. Neither, I would argue, with a few striking exceptions (most notably, his final critique of personal identity in the Appendix of T), did Hume..

- 3.3 With the possible implications of such a metacritique in mind, I (re)examine several of Hume's explicit appeals to "principles" and "establish'd maxims of metaphysics" in in some detail, and argue
- 3.4 that one can trace several useful analogies between the structure(s) of Hume's as well as Berkeley's appeals to such elenctic maxims and dialectical "principles," and 'paradoxical' metalogical arguments which have arisen in twentieth-century philosophy of logic and mathematics (principally, the theory-relative nature of notions such as 'definability' and 'consistency' and 'generality').

One consequence of this analogical study is a tentative

conjecture

- 3.5 that several of these "principles" would in fact have eventuated in a genuine metatheoretic skepticism, had Berkeley and Hume seriously applied them to (the "principles") themselves.
- 3.6 Motivated by this little complex of analogies and suggestive parallels, I also attempt to (re)consider the extremely strong, self -validating properties Hume attributed to the notion he calls "Custom," and wryly characterizes in the First Enquiry (cf. E I 55) as "a kind of preestablished harmony" and "final cause."

The principal conclusion of this line of argument are 3.6.1 that Hume's arguments for these properties eventuate in a claim which I call

"Hume's Circle:"

Only 'Custom' can establish that 'only 'Custom' can establish that

· · · · ¬¬;

and

3.6.2 that they ultimately confer so much unicity and intersubjective uniformity on our otherwise-disparate "ideas" that they form a functional bridge between Berkeley's "god," and Kant's architectonically much more elaborate claims for his notion of 'the' (?) "synthetic a priori."

Attempts to travel back and forth across this 'bridge,' in fact, form one of several recurrent themes for the book as a whole.

- 4 The chapter devoted to **Kant** is motivated in part by two remarks in the First Critique:
- 4.1 that "Verstand" ("understanding") is a "Vermögen der Einheit der Erscheinungen vermittelst der Regeln" ("capacity for unity of appearances by means of rules"), and "Vernunft" ("reason")
- a "Vermögen der Einheit der Verstandesregeln unter Prinzipien" ("capacity for unity of the rules of understanding under
- principles") (B359); and
- 4.2 that "[d]er Verstand macht für die Vernunft ebenso einen

Gegenstand aus, als die Sinnlichkeit für den Verstand"

("understanding forms just as much an object for reason, as the structure of sensibility does for understanding") (B692).

One of the chapter's principal lines of argument is an attempt to model these informal types or levels of cognition with a hierarchy of three (recursively) axiomatizable theories $S \subseteq T \subseteq U$, such that 4.2.1 S includes a set-, class- or type-theory S' strong enough to interpret the number theory and analysis needed for Newtonian dynamics (formal counterparts of Kant's "forms" of "inner" and "outer sense"), and has enough additional formal vocabulary to accommodate an appropriately Kantian theory of Anschauung(en) (intuition(s));

- 4.2.2 the consistent extension T of S includes a set-, class-, or type-theory T' strong enough to prove the (relative) consistency of S'⊆ T'; T also proves the relative consistency of S, and has enough additional vocabulary to provide a plausible if partial theory of "'the' (?) categories of the understanding;" and finally,
- 4.2.3 the consistent extension U of T includes a set-, classor type-theory U', which may or may not prove the (relative)
 consistency of T'⊆ U'; U also has enough additional vocabulary
 to provide a plausible theory of "ideas of pure reason;" but U
 may or may not, once again, prove the (relative) consistency
 of T.
- In 4.2.3, for example, we wish to leave open the possibility that U is a conservative extension of T (i. e., a consistent extension of T which proves no theorems in the language of T which are not already provable from T), in keeping with an informal assertion Kant often seems to make. Since T does not prove its own consistency, by Gödel's theorem, neither then does U.

 4.2.4 These definitions, in effect, are placeholders. They permit a great deal of latitude about the nature of S, T and U and their primed counterparts, and I offer them simply to model the idea that Kant's "understanding" involves a kind of (allegedly) canonical metatheory for his "intuition(s)," and his "reason," in turn, a not-so-canonical metatheory for "understanding" (cf. again the

quotations from B359 and B692 above).

- 4.3 Given the assumptions sketched in 4.2, we can ask whether its analogies might be aligned with (plausible counterparts of) historically Kantian claims whether, in effect, one can provide a formal miniature of significant aspects of the Kantian architectonic, and use that miniature to clarify some of the architectonic's limitations. I believe the answer to both these questions is "yes."
- 4.3.1 For a brief sample of such potential clarification, consider first the notion of the synthetic a priori, and the central claim of 'transcendental idealism,' that "[d]er Verstand schöpft seine Gesetze (a priori) nicht aus der Natur, sondern schreibt sie dieser vor" ("the understanding does not draw its laws from Nature, but prescribes them to it") (Pr 320, para. 36).

If "understanding" can be both characterized and represented by a complete theory T^* , such that S T $T^* = Th(E)$, the theory of the (allegedly) unique structure E alluded to above, then it is immediate, first, that assertions in T are substantive, 'synthetic' extensions of merely logical claims (one of the paraphrases Kant gives for "synthetic" is "erweiternd" --"extending" -- often translated wretchedly as "ampliative"). It is equally obvious, second, that since T is more comprehensive that the weaker theory S, T* must decide everything in the weaker theory S^* = the restriction of T^* to the language of S. 4.4 The more vexed underlying question, of course, is whether any sort of ('transcendental') 'deduction' could ever show that we 'must' assume (or can even "understand") the completeness of theories such as T and S, as Kant essentially claimed. or provide 'evidence' that a unique 'intended' interpretation E of T (unique at least up to elementary equivalence) 'must' 'exist.' 4.4.1 Here too, suggestive metamathematical analogies may exist. In several passages (cf., e. g., B353, B384 and B809), Kant elaborates a notion of Transzendenz, which he believes characterizes experientially unsecured "claims of reason," and which anticipates in several respects (I believe) both Georg Cantor's quasi-formal notion of class-theoretic Inkonsistenz, and later metamathematical

phenomena of incompleteness and undecidability. Kant also associates this notion explicitly at several points with an intrinsic human need to make indeterminate and overextended claims of "Vollständigkeit der Bedingungen" ("completeness of conditions") (cf., e. g., B443-444). Yet he also remarks in another passage that "die Einheit aller möglichen empirischen Verstandeshandlungen systematisch zu machen" ("making the unity of all possible empirical activities of the understanding systematic") -- which sounds like the quintessential task of any successful 'transcendental deduction' -- is "ein Geschäft der Vernunft" ("an affair of reason") (B692).

4.5 Put very briefly, I intend to explore in this chapter the hypothesis that metamathematical arguments very like those of Kant's transzendentale Dialektik put into suspension (I have in mind later uses of the German word "aufheben") claims in the transzendentaler Analytik to 'deduce' in some sense the 'existence of structures such as E. Informally. this suggests to me that Kant's claims for the structural unicity (even definability) of "Erfahrung überhaupt" ("experience in general") are inherently transzendent / inkonsistent. One way to express this conjecture is to formulate an analogue of the self-referential claim about "Custom" which I attributed earlier to Hume:

4.6 Kant's Circle:

Only synthetic a priori judgment can establish that only synthetic a priori judgment can establish that

4.7 Uncharitably, one might appeal to such formulations to conjecture that claims such as those in the Analytic must ultimately be begged (or, at one remove, that we 'must' beg that we 'must' beg them, as Kant's strangely iterative modal usages sometimes seem to suggest).

More sympathetically, one might regard them as epistemic expressions of faith, or of Blochian "hope," or of what Kant in other contexts called a "regulative ideal" -- not, in this respect at least, so very unlike Berkeley's god, or Hume's wryly proposed

"final cause" ("Custom"); or even Einstein's elusive "old man," who (allegedly) ensures for us the regularity of the physical and thought-experimental universe, and (again allegedly) does not "throw dice."

- 5 The account of the development of the forms of 'idealism' I wish to set forth in **Levels of Idealism** is recapitulated in the following remarks, which also provide a brief prototype of the book's conclusion.
- 5.1 Each of Berkeley, Hume and Kant wished to 'show' that a class of assertions (about "matter," "cause," and "experience in general," respectively) was determined by a wider class of **theoretical** data which they associated, naturally enough, with some species of intentional or 'mental' activity (for where else have any theories we have encountered come from?).
- 5.2 Each supported this 'demonstration,' further, with appeals for some sort of reductive denial of the **non**existence (or at least experiential and scientific irrelevance) of anything **not** "intentionally **in**existent" (if I may employ Brentano's later usage about 'the mental').
- 5.2.1 In this manuscript, I argue that each of these reductive claims has one or more natural metalogical analogues, but that these formal ectypes are either **inexpressible** in or **independent** of the theories to which they naturally apply. And this, in turn, suggests to me that we might do well to draw similar conclusions about their informal metaphysical prototypes.
- 5.3 Each of the three great metaphysicians I have been considering also attempted to confront the problem of the apparent nonunicity and nonuniformity of their 'merely' (?) intentional (theoretical) objects. Each had also courted this objection, in effect, by resorting to one or another of the dialectical 'modes' and 'tropes' of classical skepticism to vindicate one or another aspect of the reductionism referred to above. And each attempted to resolve the problem with some sort of ramified mixture of two characteristic

responses, one tacit and the other more explicit.

- 5.3.1 The first response was to appeal a cardinal motive of proto-idealistic metaphysics already prominently present in the writings of Anselm and Descartes: the idea that what 'conceives' something is in some sense 'greater' than (or perhaps has more 'formal reality' than) what it conceives. This argument lives on quite strongly in twentieth-century philosophy of mind, I believe, in the metaphysical pathos which seems to impel certain opponents of 'neurophilosophy' and rebutters of Turing's test.
- 5.3.2 The second response of the philosophers I have considered was essentially to relocate the unicity and uniformity most us trustingly associate with the 'objective' (?) real world in the theoretical/intentional structures to which they 'reduced' (?) it.
- 5.4 Berkeley made the second response quite straightforwardly with his appeals to the great christian "spirit," and Hume more indirectly with his dubious "preestablished harmony" of "Custom" and "Moral Science." Kant's response, in a sense, was most explicit of all, expressed by his cooptation of 'all' (?) of natural science into 'the' forms of intuition and categories of the understanding.
- also seem to me to ramify, this time in ways which may have potentially interesting implications for the philosophy of mathematics. One the one hand, all the evidence points in the direction of a rich (and to me satisfying) semantic pluralism, for any axiomatic theories of serious analogical interest. On the other, there seems to be a need for practitioners of logic to have "in mind" preferred, "intended" interpretations for such theories. And this notion seems to be recurrently metatheoretic marginal, in effect, to the fundamental (meta)theories in which we try to express it.
- 5.6 If so, this very need for logicians to postulate such recurrent metatheories, within which they can then 'locally' legimatize their (object)theoretical work (a need expressed most simply and quaintly, perhaps, in Carroll's parable of Achilles and the

Tortoise), may itself express a formal miniature of Kant's famous "Schicksal . . . der Vernunft" ("fate of reason") (A VII):

daß sie durch Fragen belästigt wird, die sie nicht abweisen kann; denn sie sind ihr durch die Natur selbst aufgegeben, die sie aber auch nicht beantworten kann; denn sie übersteigen alles Vermögen der menschlichen Vernunft.

that it is burdened by questions which it cannot brush off; for they are posed to it by the nature of reason itself, which it also, however, cannot answer; for they exceed all capacity of human reason.

5.7 And if this is so, the complex of dilemmas I have discussed may provide after all a somewhat less eloquent sense (if not meaning) to the following schematic reproduction of a cartoon I once saw on an academic's door. It depicts an apparent (baseball) box-score, of a game between the two metaphysical 'teams' which are shown below on the left:

Inning	1	2	3	4	5	6	7	8	9	Final
Realists	1	1	1	1	1	1	1	1	1	0
Idealists	0	0	0	0	0	0	0	0	0	1

	3